

1. Why does $P(A|B) = P(A)$ establish that event A and event B are independent?

2. If $P(A|B) = P(A)$, then is it always true that $P(B|A) = P(B)$? Explain.

3. Determine whether these conditional statements are independent or not.

a) What is the probability of getting a blue color on the spinner, **GIVEN THAT** a head was flipped on a coin first?

Independent or Not Independent

b) What is the probability of getting a 6 on a die, **GIVEN THAT** 6 was selected from a deck of cards?

Independent or Not Independent

c) What is the probability of getting a green marble **GIVEN THAT** a green was selected first and not replaced?

Independent or Not Independent

d) What is the probability of getting a blue color on the spinner, **GIVEN THAT** it came up blue on the last spin?

Independent or Not Independent

e) What is the probability of getting a sum of 6 on two dice, **GIVEN THAT** the roll was doubles?

Independent or Not Independent

f) What is the probability of getting a yellow marble **GIVEN THAT** a green was selected first and was replaced?

Independent or Not Independent

4. Given that event A and B are independent and

a) $P(A) = 0.4$ and $P(B) = 0.35$, then $P(A|B) =$ _____

b) $P(A) = 0.76$ and $P(B) = 0.20$, then $P(A \text{ and } B) =$ _____

c) $P(A) = 0.25$ and $P(B) = 0.25$, then $P(B|A) =$ _____

5. Given that $P(A) = 0.65$ and that the $P(A|B) = 0.5$, what can you conclude about the events A and B?

6. Using substitution mathematically demonstrate why $P(A|B) = \frac{P(A \& B)}{P(B)} = P(A)$ if the events A and B are independent.

7. Given that event A and event B are independent, determine the required probabilities.

a) $P(A \text{ and } B) = 0.4$
 $P(B) = 0.8$

$P(A) = \underline{\hspace{2cm}}$

b) $P(A | B) = 0.25$
 $P(B) = 0.5$

$P(A) = \underline{\hspace{2cm}}$

c) $P(B | A) = 0.32$
 $P(A) = 0.8$

$P(B) = \underline{\hspace{2cm}}$

d) $P(A) = 0.42$
 $P(B) = 0.4$

$P(A \text{ and } B) = \underline{\hspace{2cm}}$

e) $P(A | B) = 0.2$
 $P(B | A) = 0.4$

$P(A \text{ and } B) = \underline{\hspace{2cm}}$

f) $P(A) = 0.68$
 $P(B) = 0.4$

$P(A | B) = \underline{\hspace{2cm}}$

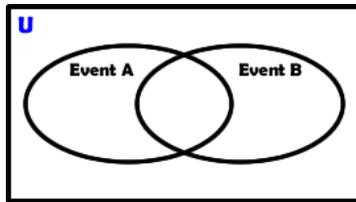
8. Determine the missing probabilities and if the two events are independent or not.

a) $P(A \text{ and } B) = 0.25$

$P(A) = 0.4$

$P(B) = 0.5$

$P(B | A) = \underline{\hspace{2cm}}$



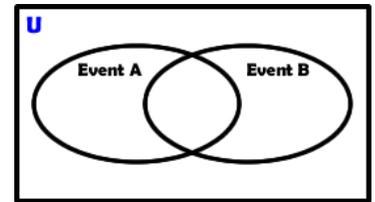
Are they independent?
 Yes or No

b) $P(A \text{ and } B) = 0.2$

$P(A) = 0.5$

$P(A \text{ or } B) = 0.7$

$P(B) = \underline{\hspace{2cm}}$



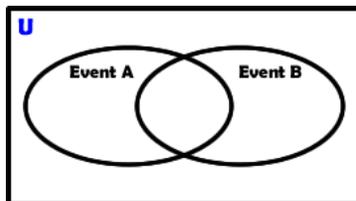
Are they independent?
 Yes or No

c) $P(A \text{ and } B) = 0.18$

$P(A \text{ not } B) = 0.4$

$P(B \text{ not } A) = 0.2$

$P(B | A) = \underline{\hspace{2cm}}$



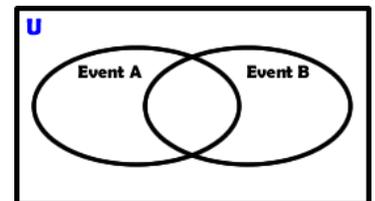
Are they independent?
 Yes or No

d) $P(A \text{ and } B) = 0.3$

$P(A) = 0.4$

$P(A \text{ or } B) = 0.85$

$P(A | B) = \underline{\hspace{2cm}}$



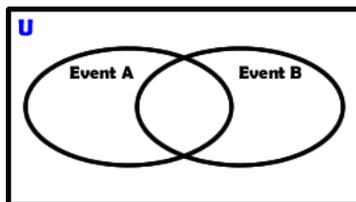
Are they independent?
 Yes or No

e) $P(A \text{ or } B) = 0.75$

$P(A) = 0.5$

$P(A \text{ and } B) = .25$

$P(B | A) = \underline{\hspace{2cm}}$



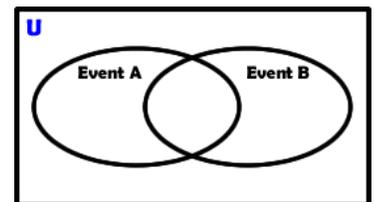
Are they independent?
 Yes or No

f) $P(A \text{ or } B) = 0.75$

$P(A) = 0.4$

$P(A \text{ and } B) = .1$

$P(A | B) = \underline{\hspace{2cm}}$



Are they independent?
 Yes or No

9. 64% of women surveyed picked Urban Life (living in a city) over Rural Life (living in the country). If gender is independent of this choice, what can you conclude about the percentage of males that would Urban life?